

An attention-based explanation for some exhaustivity operators

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 - ▶ it (partially) generates existing exhaustivity operators.

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Outline

1. Problems for the standard recipe
2. Formal, attention-based account
3. Deriving exhaustivity operators

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(*Alternative:* Hurford's constraint and local exh.)

- ▶ Hurford 1974; Katzir & Singh 2013.)

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$$\text{I-Relation}(\mathcal{Q}, p) = \mathcal{Q}(p)$$

$$\text{I-Quantity}(\mathcal{Q}, p) = \forall q \left(\left(\begin{array}{l} \text{I-Quality}(q) \wedge \\ \text{I-Relation}(\mathcal{Q}, q) \end{array} \right) \rightarrow (p \subseteq q) \right)$$

2.2. Warming-up: information-maxims

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Alternative, equivalent formulation of I-Quantity:

$$\text{I-Quantity}(\mathcal{Q}, p) = \forall q \left((\mathcal{Q}(q) \wedge p \not\subseteq q) \rightarrow \neg \Box^{\vee} q \right)$$

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- ▶ The starting point for the standard recipe.

2.3. Attention maxims

A-maxims: For an attentional intent \mathcal{A} and a QUD \mathcal{Q} :

A-Quality(\mathcal{A})

A-Relation(\mathcal{Q}, \mathcal{A})

A-Quantity(\mathcal{Q}, \mathcal{A})

2.3. Attention maxims

A-maxims: For an attentional intent \mathcal{A} and a QUD \mathcal{Q} :

A-Quality(\mathcal{A}) = $\forall a (\mathcal{A}(a) \rightarrow \diamond^{\vee} a)$ *(first attempt)*

A-Relation(\mathcal{Q}, \mathcal{A})

A-Quantity(\mathcal{Q}, \mathcal{A})

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A-maxims: For an attentional intent \mathcal{A} and a QUD \mathcal{Q} :

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$$\text{A-Quantity}(\mathcal{Q}, \mathcal{A}) = \forall a ((\mathcal{Q}(a) \wedge \neg \mathcal{A}(a)) \rightarrow \neg \diamond^{\vee} a)$$

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Not quite right, e.g.:

(2) Who (of John, Mary and Bill) was at the party?

c. John, or everyone.

(Exh.: if Mary/Bill, then everyone.)

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Better:

(2) Who (of John, Mary and Bill) was at the party?

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2.4. Illustration of A-maxims

- (2) a. John. (*Exh.: not Mary or Bill.*)
b. John, or both John and Mary. (*Exh.: not Bill.*)
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2.4. Illustration of A-maxims

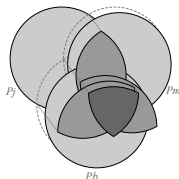
- (2) a. John. (*Exh.: not Mary or Bill.*)
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Let $\mathcal{Q} = \{\wedge Pj, \wedge Pm, \wedge Pb, \dots\}$ (closed under intersection)

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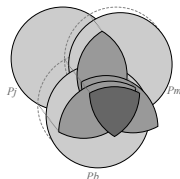
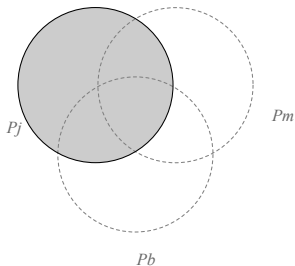


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Let $\mathcal{Q} = \{\wedge P_j, \wedge P_m, \wedge P_b, \dots\}$ (closed under intersection), and:

- (2a): $\mathcal{A} = \{\wedge P_j\}$;

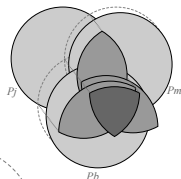
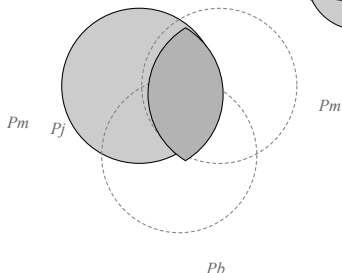
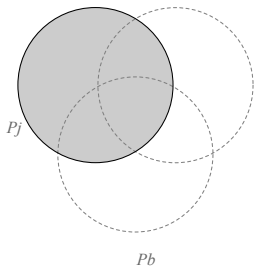


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- ▶ (2a): $\mathcal{A} = \{\wedge P_j\}$;
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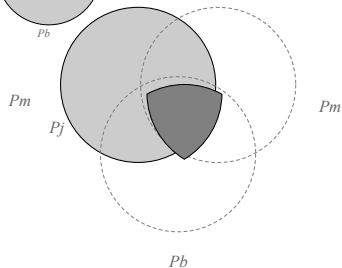
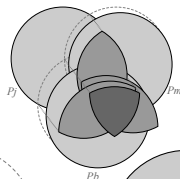
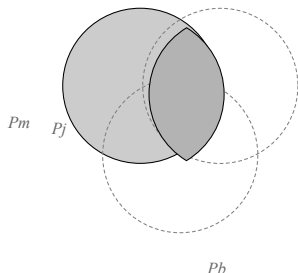
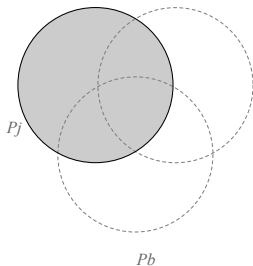


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- ▶ (2a): $\mathcal{A} = \{\wedge P_j\}$;
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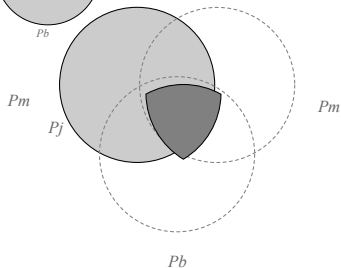
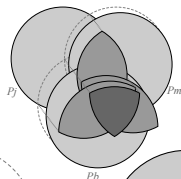
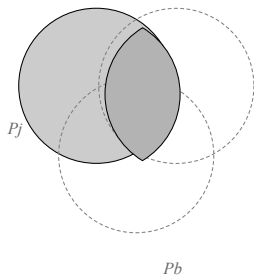
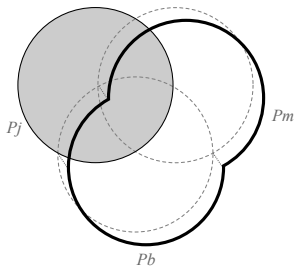


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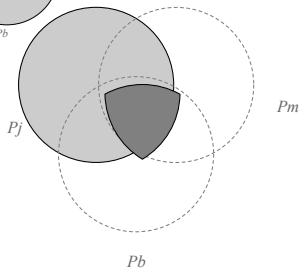
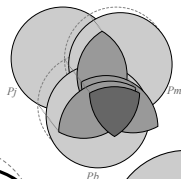
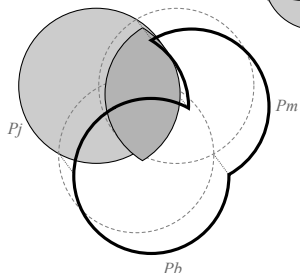
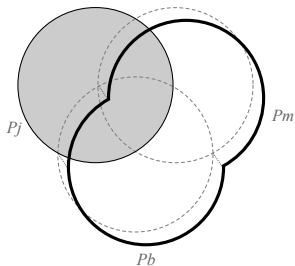


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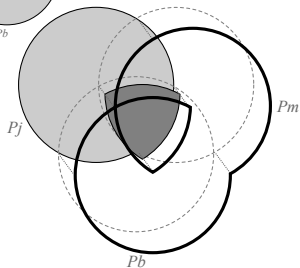
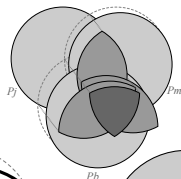
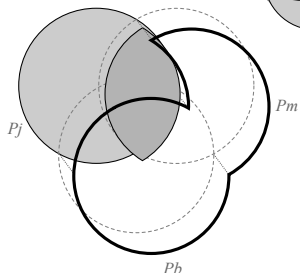
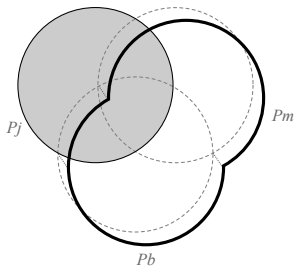


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Fact: For all admissible models \mathbf{M} that interpret \mathcal{Q} , \mathcal{A} as above:

- ▶ (2a): $\mathbf{M} \models \text{A-Quantity}(\mathcal{Q}, \mathcal{A}) = (\Box \neg Pm \wedge \Box \neg Pb)$
- ▶ (2b):
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b. John, or both John and Mary. (*Exh.: not Bill.*)
c. John, or everyone. (*Exh.: if Mary/Bill, then everyone.*)

Let $\mathcal{Q} = \{\wedge Pj, \wedge Pm, \wedge Pb, \dots\}$ (closed under intersection)

- ▶ (2a): $\mathcal{A} = \{\wedge Pj\}$;
- ▶ (2b): $\mathcal{A} = \{\wedge Pj, \wedge(Pj \wedge Pm)\}$;
- ▶ (2c): $\mathcal{A} = \{\wedge Pj, \wedge(Pj \wedge Pm \wedge Pb)\}$.

Fact: For all admissible models \mathbf{M} that interpret \mathcal{Q} , \mathcal{A} as above:

- ▶ (2a): $\mathbf{M} \models \text{A-Quantity}(\mathcal{Q}, \mathcal{A}) = (\Box \neg Pm \wedge \Box \neg Pb)$
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Outline

1. Problems for the standard recipe
2. Formal, attention-based account
3. Deriving exhaustivity operators

Conclusion

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Repeated:

$$\text{A-Quantity}(\mathcal{Q}, \mathcal{A}) = \forall a \left(\begin{array}{l} ((\mathcal{Q}(a) \wedge \neg \mathcal{A}(a)) \rightarrow \\ \neg^{\vee} a \vee \\ \square \left(\exists b (\mathcal{A}(b) \wedge (b \subset a) \wedge \vee b) \right) \end{array} \right)$$

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$$\text{EXH}(Q, \mathcal{A}) = \wedge \forall a \left(\begin{array}{l} ((Q(a) \wedge \neg \mathcal{A}(a)) \rightarrow \\ (\neg^{\forall} a \vee \exists b (\mathcal{A}(b) \wedge (b \subset a) \wedge \vee b)) \end{array} \right)$$

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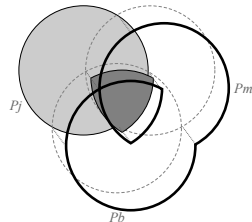
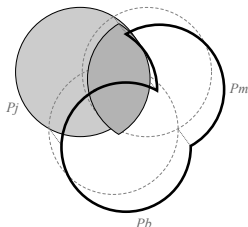
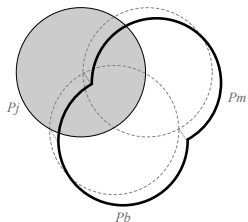
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Alternative, equivalent definition:

$$\text{EXH}(Q, \mathcal{A}) = \bigcap_{\substack{a \in Q \\ a \notin \mathcal{A}}} (\bar{a} \cup \bigcup_{\substack{b \in \mathcal{A} \\ b \subset a}} b)$$

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The basic idea (Van Rooij & Schulz 2006; Spector 2007):

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- ▶ my account makes very different predictions (e.g., problems A.-D.).

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But again: empirically our accounts make very different predictions.

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- ▶ the predicted implications are technically similar to the patterns described by (some) existing operators.

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